

System Validation: Hennessy-Milner Logic

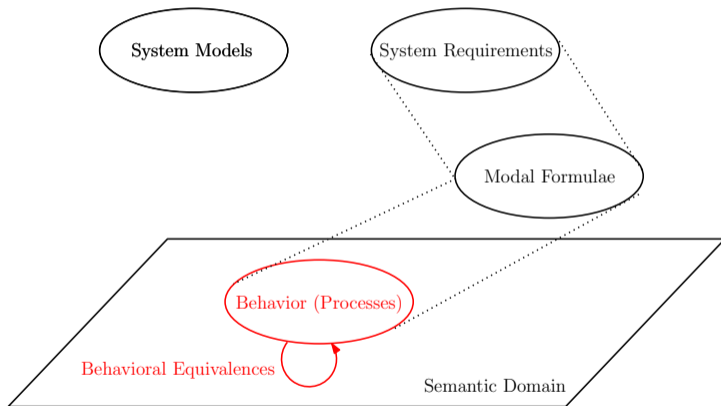
Mohammad Mousavi and Jeroen Keiren



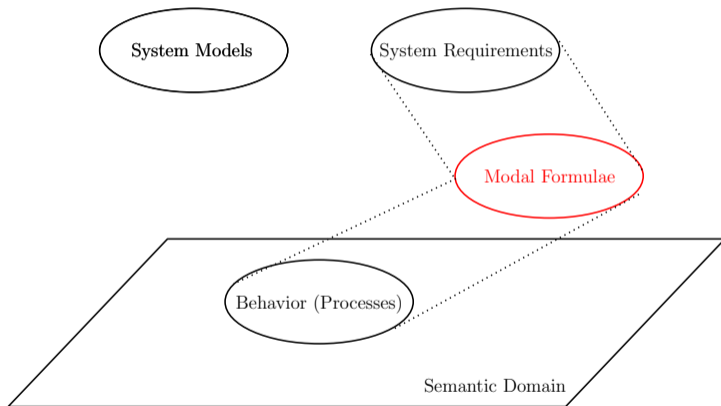
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General Overview



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Motivation

Drawbacks of verification using behavioural equivalences:

- ▶ Complex behaviour of specification

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Solution: express properties **outside** of behaviour

Observable Events

- ▶ Fix **observable** events (interactions with external world)



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- ▶ Describe **temporal properties** using these
- ▶ **Verify correctness** of properties with respect to some LTS

Observable Events: Examples

A scientist **interacts with environment**

- ▶ *coffee* for taking coffee in

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- ▶ the scientist is not willing to drink coffee now
- ▶ the scientist is willing to drink both coffee and tea now
- ▶ the scientist will always produce a publication immediately after drinking two coffees in a row

Hennessy-Milner logic

Syntax

For $a \in Act$, Hennessy-Milner formulas φ, ψ are the following:

true holds in every state

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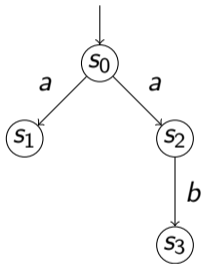
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Algorithm

- ▶ Identify all subformulas
- ▶ Label states with subformulas they satisfy, starting from the smallest subformula (*true*)

Examples

Is the HML formula $\langle a \rangle \langle b \rangle \text{true}$ satisfied by the labelled transition system (i.e., by its **initial state**)?

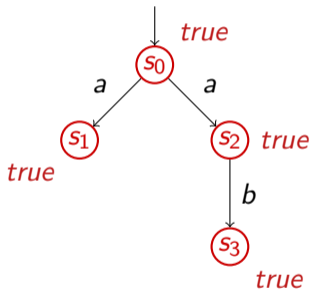


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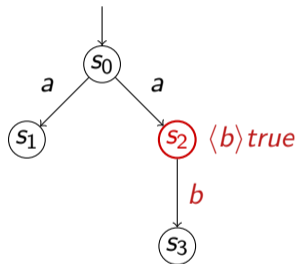
true

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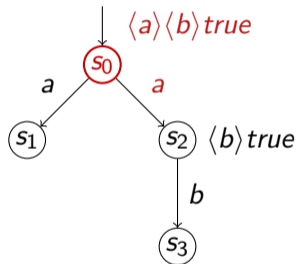


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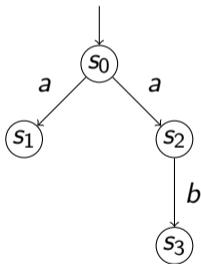


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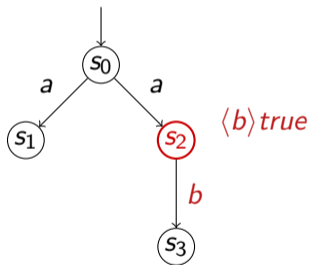
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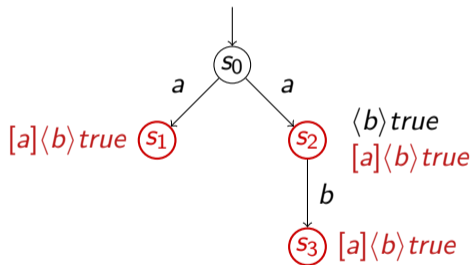
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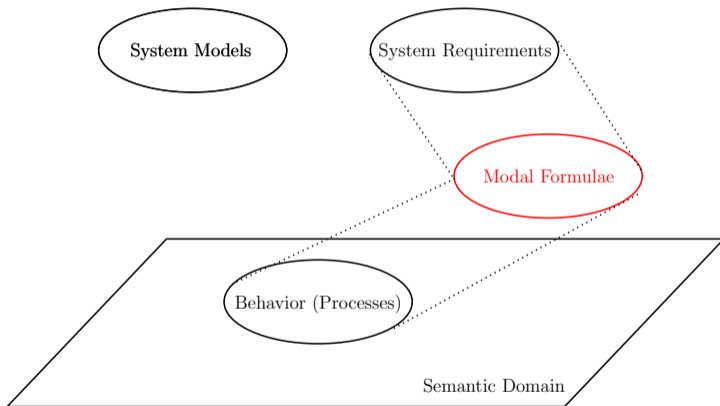
Observations

There are relevant properties that cannot be expressed in HML. HML is restricted to a **finite depth**.

Summary

- ▶ Behavioural equivalences not always suitable for verification
- ▶ **Hennessy-Milner logic** provides alternative way to describe properties
- ▶ Only properties of **finite depth** can be described

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Thank you very much.